Applying Subsequence Matching to Collaborative Filtering

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V Congreso Español de Recuperación de Información (CERI 2018)



- Recommender Systems
- 2 Sequential similarities





Outline

Recommender Systems

2 Sequential similarities

3 Experiments



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Recommender Systems



• Suggest new items to users based on their tastes and needs

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- Different methods to make recommendations (content-based, collaborative filtering, hybrids)

Recommender Systems



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- Different methods to make recommendations (content-based, collaborative filtering, hybrids)
- We will focus on neighborhood based collaborative filtering algorithms

	i_1	<i>i</i> 2	i ₃	i ₄	•••
u_1	-	-	5	3	
<i>u</i> ₂	4	-	4	-	
Из	5	5	-	-	
U ₄	-	2	1	-	
<i>и</i> 5	2	-	-	5	
и ₆	-	1	-	1	
			• • •	• • •	• • •

	i_1	i ₂	i ₃	i ₄	
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- Normally the User × Item matrix is very sparse (90%-99% of empty values)
- Collaborative filtering try to fill the matrix either with latent factor models or neighborhood approaches

Matrix factorization techniques

$$\min_{p*,q*} \sum_{u,i\in R} (r_{ui} - q_i^T p_u)^2 + \lambda(||q_i||^2 + ||p_u||^2)$$

(1)

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- q_i and p_u are the latent vectors of the user u and the item i
- R denotes all the training samples
- λ is the regularization parameter

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Neighborhood approaches $s_{u,i} \propto \sum_{v \in N_i(u)} w_{uv} r_{vi}$ (2)

- r_{vi} is the rating of the neighbour v
- w_{uv} is the similarity between user u and v

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Classic similarities

Pearson correlation

$$\mathsf{PC}(u,v) = \frac{\sum_{i \in \mathcal{I}_{uv}} (r_{ui} - \overline{r}_u)(r_{vi} - \overline{r}_v)}{\sqrt{\sum_{i \in \mathcal{I}_{uv}} (r_{ui} - \overline{r}_u)^2 \sum_{i \in \mathcal{I}_{uv}} (r_{vi} - \overline{r}_v)^2}}$$
(3)

Cosine similarity

$$\cos(u, v) = \frac{\sum_{i \in \mathcal{I}_{uv}} r_{ui} r_{vi}}{\sqrt{\sum_{i \in \mathcal{I}_u} r_{ui}^2 \sum_{j \in \mathcal{I}_v} r_{vj}^2}}$$
(4)

Jaccard index

$$\mathsf{Jaccard}(\mathsf{u},\mathsf{v}) = rac{|I_u \cap I_v|}{|I_u \cup I_u|}$$

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- Find the longest common subsequence (list of elements not necessary consecutive but maintaining the order) between 2 strings X and Y
- Used in DNA sequencing and file comparison
- Can be resolved applying dynamic programming filling a matrix of size $(|X|+1) \times (|Y|+1)$

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Longest Common Subsequence

$$\mathcal{L}[i,j] = \begin{cases} 0 & \text{if } i=0 \text{ or } j=0\\ \mathcal{L}[i-1,j-1]+1 & \text{if } i,j>0 \text{ and } X_i = Y_j \\ \max(\mathcal{L}[i,j-1],\mathcal{L}[i-1,j]) & \text{if } i,j>0 \text{ and } X_i \neq Y_j \end{cases}$$
(6)

• The last position in the matrix contains the length of the longest common subsequence

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 - Using the value of the interaction, i.e., $f_r: I(u) \to \mathcal{R}, f_r(x) = x(r).$
 - Using a combination of the item and the interaction value, i.e., $f_{ir}: I(u) \rightarrow \mathcal{I} \times \mathcal{R}, f_{ir}(x) = (x(i), x(r)).$

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- We used integers as symbols for the transformations
- These transformations generate a pure collaborative filtering approach but they are easily extensible to use content information





Table: Interaction (ratings) data between two users and five items.



Table: Representation of the interactions for different transformation functions

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$$sim_1^{f,\delta} = LCS_CF(u, v, f, \delta)$$

$$sim_2^{f,\delta} = (sim_1^{f,\delta})^2 / (|f(u)| \cdot |f(v)|)$$
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• Using the pure item transformation (*f_i*) and a global ordering, we obtain an equivalence with the binary cosine:

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• For more information, see Bellogín and Sánchez (2017)

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Toy example

Movie (id)	Director (id)	Genres (ids)	u_1	<i>u</i> ₂
The Wild Bunch (M1)	Sam Peckinpah (D1)	Western (G1) Robbery (G2)	5	
Seven Samurais (M2)	Akira Kurosawa (D2)	Drama (G4) Adventure (G5)	4	5
The Iron Cross (M3)	Sam Peckinpah (D1)	War (G6)}	3	
Gladiator (M4)	Riddley Scott (D3)	Action (G3) Drama (G4) Adventure (G5)	4	2
Alien (M5)	Riddley Scott (D3)	Sci-Fi (G7)		5
The Magnificent Seven (M8)	John Sturges (D4)	Western (G1) Adventure (G5)		4

• $f_i: u_1 = (1, 2, 3, 4), u_2 = (2, 4, 5, 8)$

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$$f_i: u_1 = (1, 2, 3, 4), u_2 = (2, 4, 5, 8)$$

• $sim_1 = 2, sim_2 = 0.25$
• $f_{ir}: u_1 = (15, 24, 33, 44), u_2 = (25, 42, 55, 84)$
• $\delta = 1, sim_1 = 1, sim_2 = 1/16$
• $\delta = 0, sim_1 = 0, sim_2 = 0$

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Table: Statistics	about	the	datasets	used	in	the experiments.
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Dataset	users	items	ratings	Density
Lastfm HetRec	1,892	17,632	92, 834	0.28%
MovieLens HetRec	2,113	10,197	855, 598	3.97%

- 5-fold cross-validation
- Analyze both relevance (Precision, MAP, nDCG and Recall) and novelty and diversity, cutoff @5
- Reported results from RankSys and Mahout frameworks
- Different baselines analyzed: Popularity, UB (different similarities, including JMSD from Bobadilla et al. (2010)), IB (different similarities), MF (HKV version from Hu et al. (2008))



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- In Movielens, LCS is better than most baselines, except for the HKV and two UB approaches
- Very different performance between RankSys and Mahout frameworks

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Conclusions

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- We have shown that the basic approach is equivalent to the binary cosine similarity metric
- Our approach is competitive in two datasets with respect to other state-of-the-art algorithms in relevance, novelty, and diversity metrics
- Our LCS-based similarity can be easily extended to use content-based and temporal information allowing us to model the user profiles better

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- The LCS algorithm can be also used in evaluation, to assess the quality of the recommendations when considering the ordering of the user interactions in the test set

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Thank you

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Experiments. Lastfm: RankSys



Figure: Performance results in the Lastfm dataset for RankSys framework.

Experiments. Lastfm: Mahout



Figure: Performance results in the Lastfm dataset for Mahout framework.

Experiments. Movielens: RankSys



Figure: Performance results in the <u>MovieLens dataset</u> for RankSys framework.

Experiments. Movielens: Mahout



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- Bellogín, A. and Sánchez, P. (2017). Collaborative filtering based on subsequence matching: A new approach. *Inf. Sci.*, 418:432–446.
 Bobadilla, J., Serradilla, F., and Bernal, J. (2010). A new collaborative filtering metric that improves the behavior of recommender systems. *Knowl.-Based Syst.*, 23(6):520–528.
 Hu, X., Koren, X., and Volinsky, C. (2008). Collaborative filtering for
- Hu, Y., Koren, Y., and Volinsky, C. (2008). Collaborative filtering for implicit feedback datasets. In *Proceedings of the 8th IEEE International Conference on Data Mining (ICDM 2008), December* 15-19, 2008, Pisa, Italy, pages 263–272. IEEE Computer Society.