# Applying Subsequence Matching to Collaborative Filtering 

Alejandro Bellogín<br>Pablo Sánchez

Universidad Autónoma de Madrid
Escuela Politécnica Superior
Departamento de Ingeniería Informática
V Congreso Español de
Recuperación de Información (CERI 2018)

## Outline

(1) Recommender Systems
(2) Sequential similarities
(3) Experiments
(4) Conclusions and future work

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(1) Recommender Systems

## (2) Sequential similarities

(3) Experiments

## 4 Conclusions and future work

## Recommender Systems



- Suggest new items to users based on their tastes and needs


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- Different methods to make recommendations (content-based, collaborative filtering, hybrids)


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- Suggest new items to users based on their tastes and needs
- Different methods to make recommendations (content-based, collaborative filtering, hybrids)
- We will focus on neighborhood based collaborative filtering algorithms


## Collaborative filtering

|  | $i_{1}$ | $i_{2}$ | $i_{3}$ | $i_{4}$ | $\cdots$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $u_{1}$ | - | - | 5 | 3 | $\cdots$ |
| $u_{2}$ | 4 | - | 4 | - | $\cdots$ |
| $u_{3}$ | 5 | 5 | - | - | $\cdots$ |
| $u_{4}$ | - | 2 | 1 | - | $\cdots$ |
| $u_{5}$ | 2 | - | - | 5 | $\cdots$ |
| $u_{6}$ | - | 1 | - | 1 | $\cdots$ |
| $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ |

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| $u_{2}$ | 4 | - | 4 | - | $\cdots$ |
| $u_{3}$ | 5 | 5 | - | - | $\cdots$ |
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- Normally the User $\times$ Item matrix is very sparse (90\%-99\% of empty values)
- Collaborative filtering try to fill the matrix either with latent factor models or neighborhood approaches


## Collaborative filtering

## Matrix factorization techniques

$$
\begin{equation*}
\min _{p *, q *} \sum_{u, i \in R}\left(r_{u i}-q_{i}^{T} p_{u}\right)^{2}+\lambda\left(\left\|q_{i}\right\|^{2}+\left\|p_{u}\right\|^{2}\right) \tag{1}
\end{equation*}
$$

- $q_{i}$ and $p_{u}$ are the latent vectors of the user $u$ and the item $i$
- $R$ denotes all the training samples
- $\lambda$ is the regularization parameter


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Neighborhood approaches

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\begin{equation*}
s_{u, i} \propto \sum_{v \in N_{i}(u)} w_{u v} r_{v i} \tag{2}
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- $r_{v i}$ is the rating of the neighbour $v$
- $w_{u v}$ is the similarity between user $u$ and $v$


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## Classic similarities

## Pearson correlation

$$
\begin{equation*}
\operatorname{PC}(u, v)=\frac{\sum_{i \in \mathcal{I}_{u v}}\left(r_{u i}-\bar{r}_{u}\right)\left(r_{v i}-\bar{r}_{v}\right)}{\sqrt{\sum_{i \in \mathcal{I}_{u v}}\left(r_{u i}-\bar{r}_{u}\right)^{2} \sum_{i \in \mathcal{I}_{u v}}\left(r_{v i}-\bar{r}_{v}\right)^{2}}} \tag{3}
\end{equation*}
$$

Cosine similarity

$$
\begin{equation*}
\cos (u, v)=\frac{\sum_{i \in \mathcal{I}_{u v}} r_{u i} r_{v i}}{\sqrt{\sum_{i \in \mathcal{I}_{u}} r_{u i}^{2} \sum_{j \in \mathcal{I}_{v}} r_{v j}^{2}}} \tag{4}
\end{equation*}
$$

Jaccard index

$$
\begin{equation*}
\operatorname{Jaccard}(u, v)=\frac{\left|I_{u} \cap I_{v}\right|}{\left|I_{u} \cup I_{u}\right|} \tag{5}
\end{equation*}
$$

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## Longest Common Subsequence (LCS)

- Find the longest common subsequence (list of elements not necessary consecutive but maintaining the order) between 2 strings $X$ and $Y$
- Used in DNA sequencing and file comparison
- Can be resolved applying dynamic programming filling a matrix of size $(|X|+1) \times(|Y|+1)$


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## Longest Common Subsequence

$$
L[i, j]= \begin{cases}0 & \text { if } i=0 \text { or } j=0  \tag{6}\\ L[i-1, j-1]+1 & \text { if } i, j>0 \text { and } X_{i}=Y_{j} \\ \max (L[i, j-1], L[i-1, j]) & \text { if } i, j>0 \text { and } X_{i} \neq Y_{j}\end{cases}
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- The last position in the matrix contains the length of the longest common subsequence


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$\emptyset \quad A \quad G \quad G \quad T \quad A C$
Ø
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| $\emptyset$ | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| $G$ |  |  |  |  |  |  |  |
| C |  |  |  |  |  |  |  |
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C $\begin{array}{llllllll} & 0 & 0 & 1 & 1 & 1 & 1 & 2\end{array}$

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- Using the item, i.e., $f_{i}: I(u) \rightarrow \Sigma=\mathcal{I}, f_{i}(x)=x(i)$.
- Using the value of the interaction, i.e., $f_{r}: I(u) \rightarrow \mathcal{R}, f_{r}(x)=x(r)$.
- Using a combination of the item and the interaction value, i.e., $f_{i r}: I(u) \rightarrow \mathcal{I} \times \mathcal{R}, f_{i r}(x)=(x(i), x(r))$.


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- We used integers as symbols for the transformations
- These transformations generate a pure collaborative filtering approach but they are easily extensible to use content information


## Toy example



Table: Interaction (ratings) data between two users and five items.

| $f$ | $f(u)$ | $f(v)$ |
| :---: | :---: | :---: |
| $f_{i}$ | $(X, \triangle, \square, \diamond)$ | $(X, \bigcirc, \square, \diamond)$ |
| $f_{r}$ | $(4,5,3,1)$ | $(4,5,4,4)$ |
| $f_{i r}$ | $\left(\times 4, \triangle 5, \square 3, \diamond_{1)}\right.$ | $(\times 4, \bigcirc 5, \square 4, \diamond 4)$ |

Table: Representation of the interactions for different transformation functions

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- Normalize the value LCS in the $[0,1]$ interval

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\begin{gather*}
\operatorname{sim}_{1}^{f, \delta}=\operatorname{LCS} C F(u, v, f, \delta)  \tag{8}\\
\operatorname{sim}_{2}^{f, \delta}=\left(\operatorname{sim}_{1}^{f, \delta}\right)^{2} /(|f(u)| \cdot|f(v)|) \tag{9}
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- Using the pure item transformation $\left(f_{i}\right)$ and a global ordering, we obtain an equivalence with the binary cosine:

$$
\begin{equation*}
\cos _{b}(u, v)=|I(u, v)| / \sqrt{(|f(u)| \cdot|f(v)|)} \tag{10}
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\begin{gather*}
\operatorname{sim}_{1}^{f, \delta}=\operatorname{LCS} C F(u, v, f, \delta)  \tag{8}\\
\operatorname{sim}_{2}^{f, \delta}=\left(\operatorname{sim}_{1}^{f, \delta}\right)^{2} /(|f(u)| \cdot|f(v)|) \tag{9}
\end{gather*}
$$

- Using the pure item transformation $\left(f_{i}\right)$ and a global ordering, we obtain an equivalence with the binary cosine:

$$
\begin{equation*}
\cos _{b}(u, v)=|I(u, v)| / \sqrt{(|f(u)| \cdot|f(v)|)} \tag{10}
\end{equation*}
$$

- For more information, see Bellogín and Sánchez (2017)


## Toy example

| Movie (id) | Director (id) | Genres (ids) | $u_{1}$ | $u_{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| The Wild Bunch (M1) | Sam Peckinpah (D1) | $\left.\begin{array}{l} \text { Western (G1) } \\ \text { Robbery (G2) } \end{array}\right\}$ | 5 |  |
| Seven Samurais (M2) | Akira Kurosawa (D2) | $\left.\begin{array}{l} \text { Action (G3) } \\ \text { Drama (G4) } \\ \text { Adventure (G5) } \end{array}\right\}$ | 4 | 5 |
| The Iron Cross (M3) | Sam Peckinpah (D1) | War (G6) \} <br> Action (G3) | 3 |  |
| Gladiator (M4) | Riddley Scott (D3) | $\left.\begin{array}{l}\text { Drama (G4) } \\ \text { Adventure (G5) }\end{array}\right\}$ | 4 | 2 |
| Alien (M5) | Riddley Scott (D3) | $\left.\begin{array}{l} \text { Sci-Fi (G7) } \\ \text { Terror (G8) } \end{array}\right\}$ |  | 5 |
| The Magnificent Seven (M8) | John Sturges (D4) | $\left.\begin{array}{l} \text { Western (G1) } \\ \text { Adventure (G5) } \end{array}\right\}$ |  | 4 |

- $f_{i}: u_{1}=(1,2,3,4), u_{2}=(2,4,5,8)$
- $f_{i r}: u_{1}=(15,24,33,44), u_{2}=(25,42,55,84)$


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- $f_{i}: u_{1}=(1,2,3,4), u_{2}=(2,4,5,8)$
- $\operatorname{sim}_{1}=2, \operatorname{sim}_{2}=0.25$
- $f_{i r}: u_{1}=(15,24,33,44), u_{2}=(25,42,55,84)$
- $\delta=1, \operatorname{sim}_{1}=1, \operatorname{sim}_{2}=1 / 16$
- $\delta=0, \operatorname{sim}_{1}=0, \operatorname{sim}_{2}=0$


## Outline

## (1) Recommender Systems

## (2) Sequential similarities

(3) Experiments

## 4 Conclusions and future work

## Experiments

Table: Statistics about the datasets used in the experiments.

| Dataset | users | items | ratings | Density |
| :---: | ---: | ---: | ---: | ---: |
| Lastfm HetRec | 1,892 | 17,632 | 92,834 | $0.28 \%$ |
| MovieLens HetRec | 2,113 | 10,197 | 855,598 | $3.97 \%$ |

- 5-fold cross-validation
- Analyze both relevance (Precision, MAP, nDCG and Recall) and novelty and diversity, cutoff @5
- Reported results from RankSys and Mahout frameworks
- Different baselines analyzed: Popularity, UB (different similarities, including JMSD from Bobadilla et al. (2010)), IB (different similarities), MF (HKV version from Hu et al. (2008))


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- In Movielens, LCS is better than most baselines, except for the HKV and two UB approaches
- Very different performance between RankSys and Mahout frameworks


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## Conclusions

- We have defined a new UB similarity based on the LCS algorithm
- We have shown that the basic approach is equivalent to the binary cosine similarity metric
- Our approach is competitive in two datasets with respect to other state-of-the-art algorithms in relevance, novelty, and diversity metrics
- Our LCS-based similarity can be easily extended to use content-based and temporal information allowing us to model the user profiles better


## Future work

- The LCS-based similarity may incorporate repetitions in a natural way


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- The LCS-based similarity may incorporate repetitions in a natural way
- Perform experiments considering both content-based and temporal information
- The LCS algorithm can be also used in evaluation, to assess the quality of the recommendations when considering the ordering of the user interactions in the test set


# Applying Subsequence Matching to Collaborative Filtering 

Alejandro Bellogín Pablo Sánchez

Universidad Autónoma de Madrid<br>Escuela Politécnica Superior<br>Departamento de Ingeniería Informática<br>V Congreso Español de<br>Recuperación de Información (CERI 2018)

## Thank you

## Experiments. Lastfm: RankSys



RankSys

Performance metrics

RankSys

Non-performance metrics

Figure: Performance results in the Lastfm dataset for RankSys framework.

## Experiments. Lastfm: Mahout



Performance metrics

Mahout


Non-performance metrics -

Figure: Performance results in the Lastfm dataset for Mahout framework.

## Experiments. Movielens: RankSys



Figure: Performance results in the MovieLens dataset for RankSys framework.

## Experiments. Movielens: Mahout



Figure: Performance results in the MovieLens dataset for RankSys framework.

## References I

Bellogín, A. and Sánchez, P. (2017). Collaborative filtering based on subsequence matching: A new approach. Inf. Sci., 418:432-446.
Bobadilla, J., Serradilla, F., and Bernal, J. (2010). A new collaborative filtering metric that improves the behavior of recommender systems. Knowl.-Based Syst., 23(6):520-528.
Hu, Y., Koren, Y., and Volinsky, C. (2008). Collaborative filtering for implicit feedback datasets. In Proceedings of the 8th IEEE International Conference on Data Mining (ICDM 2008), December 15-19, 2008, Pisa, Italy, pages 263-272. IEEE Computer Society.

